

# Pulse Dampener Size Analysis

Part I - Required Compliant Gas Volume Calculation

Part II - Additional Attenuation Using a Series Flow Resistance

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# Goals

## Part I:

It is desired to learn the required enclosed gas volume for a pressure pulse dampener for use with small motor driven diaphragm pumps.

An equation is derived for calculating the required volume as a function of pump stroke volume, allowable maximum pressure pulse amplitude and absolute pump-up pressure.

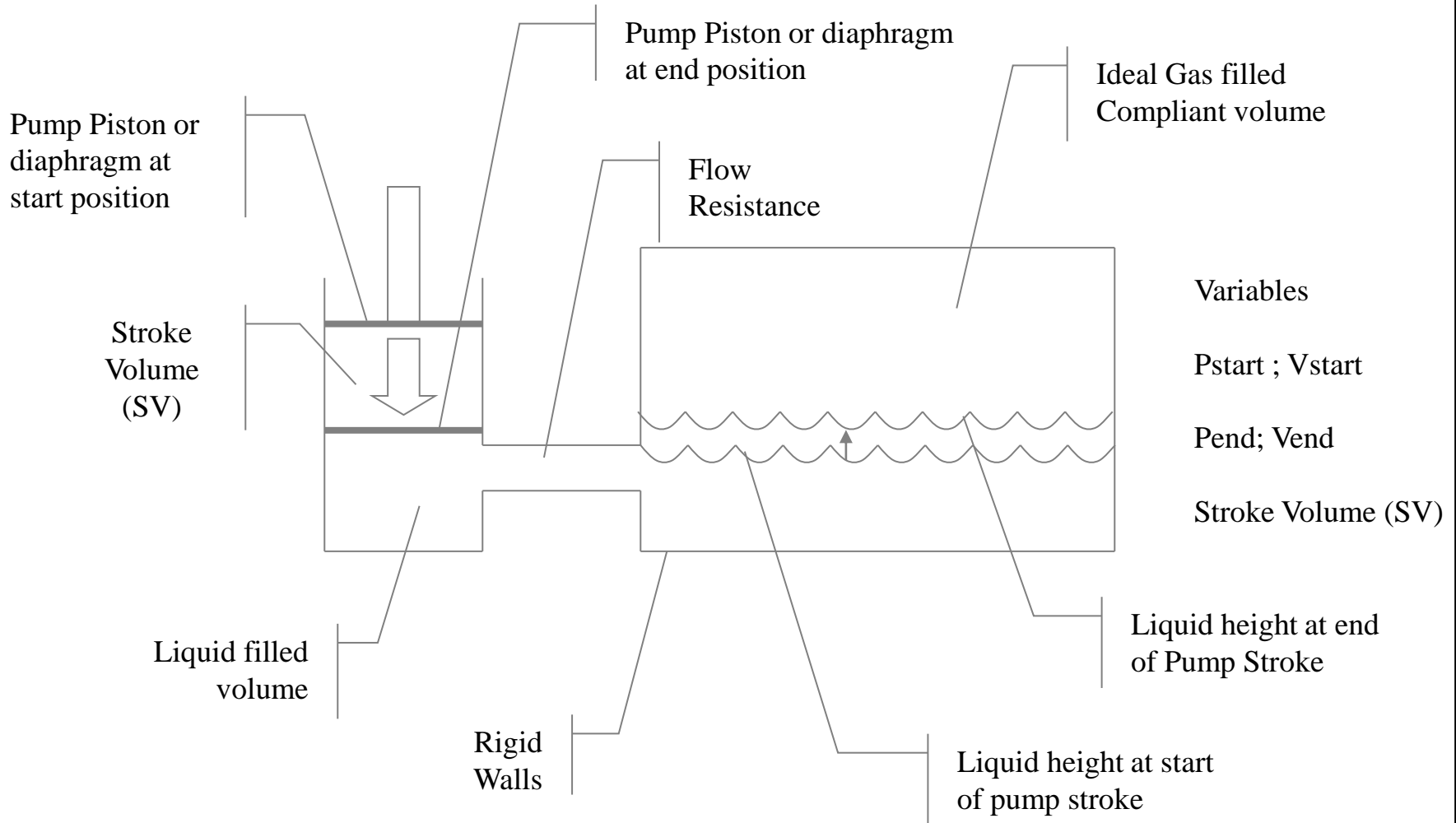
The results for this expression are presented in graphic format for use by pressure pulse dampener designers.

## Part II:

Calculation of the frequency vs. pressure pulse amplitude roll-off rate as a function of compliant volume and series flow resistance, is needed.

Suitable equations and useful display graphs are presented that can help the pulse dampener designer produce an optimized resultant pulse dampening device.

# Scenario for Analysis



# Use Boyle's Law to Solve for Required Initial Volume

Variables:	$P_{start}$ ; $V_{start}$	$P_{end}$ ; $V_{end}$	
Assume:	$P_{start}$	$P_{pulse}$ = pulse amplitude	$SV$ = Stroke Volume
Solve for:	$V_{start}$ = required pulse dampener volume		

Boyle's Law (Isothermal ideal gas law):  $P_{start} * V_{start} = P_{end} * V_{end}$

Let:  $V_{end} = V_{start} - SV$      $P_{end} = P_{start} + P_{pulse}$     Stroke Volume (SV) =  $V_{start} - V_{end}$

Then:  $V_{start} = (P_{end}/P_{start}) * V_{end} = \{ (P_{start} + P_{pulse}) * (V_{start} - SV) \} / P_{start}$

After some algebra:

$$V_{start} = (1 + P_{start} / P_{pulse}) * SV$$

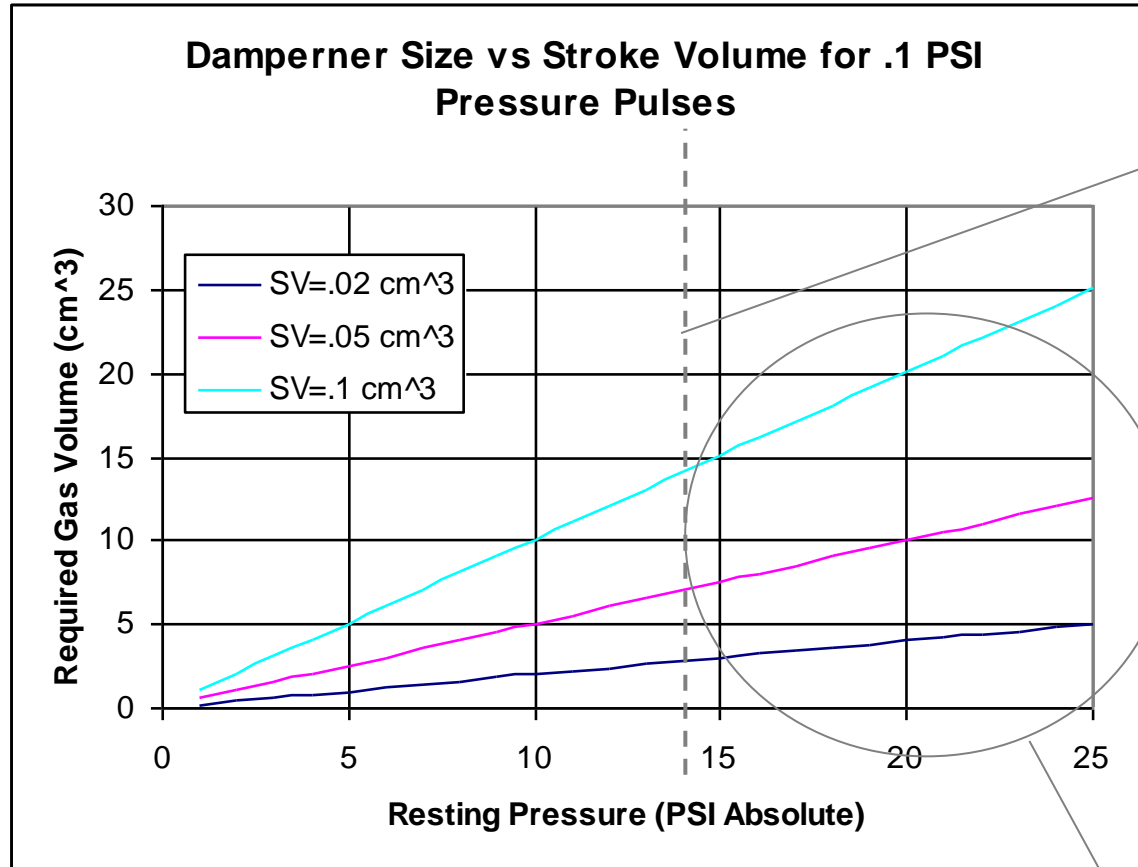
Example:

let  $P_{start} = 17$  PSI absolute     $P_{pulse} = .1$  PSI     $SV = .05$  cm<sup>3</sup>

then Required  $V_{start}$  (gas volume in dampener) = 8.55 cm<sup>3</sup>

thus Compliance = C = .05 cm<sup>3</sup> / .1 PSI = .5 cm<sup>3</sup> / PSI

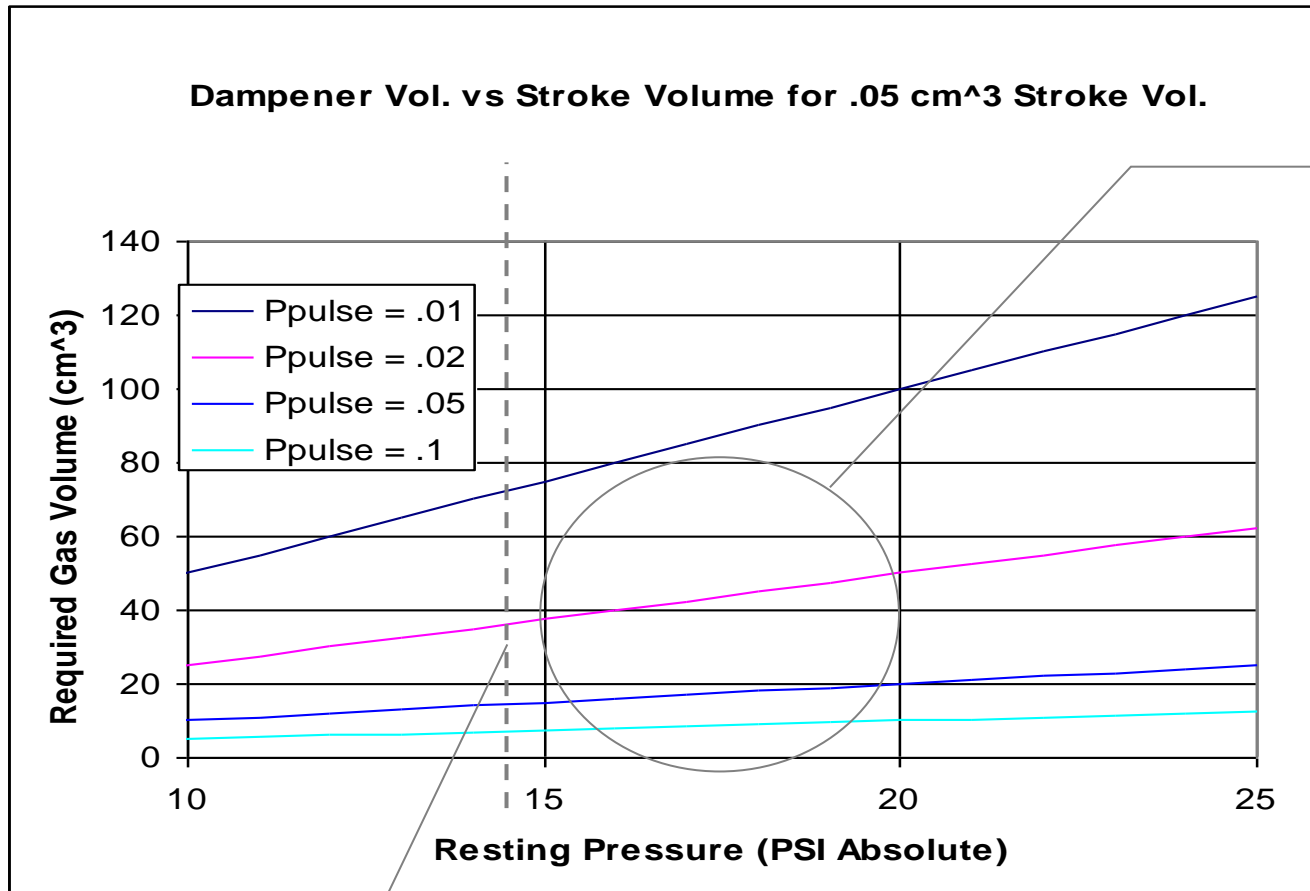
# Required Pulse Dampener Volume



One  
Atmosphere

Region of  
Interest

# Required Pulse Dampener Volume



Region of Interest

One  
Atmosphere

# Conclusions – Part I

1. It seems that at least 10 cm<sup>3</sup> gas volume will be needed to “snub” Model XYZ Diaphragm pump pressure pulses to about .1 PSI
2. It seems that 25 cm<sup>3</sup> gas volume would be the largest needed.
3. Use of a fluidic resistor or small feed port restrictors ahead of the dampener could possibly reduce these calculated volumes by a factor of 2 before average pressure drops in the resistor or port restrictors becomes a problem.
4. Reduction of pulse amplitudes by fluid resistances and compliance within downstream system elements might allow further diminishment of downstream pressure pulse

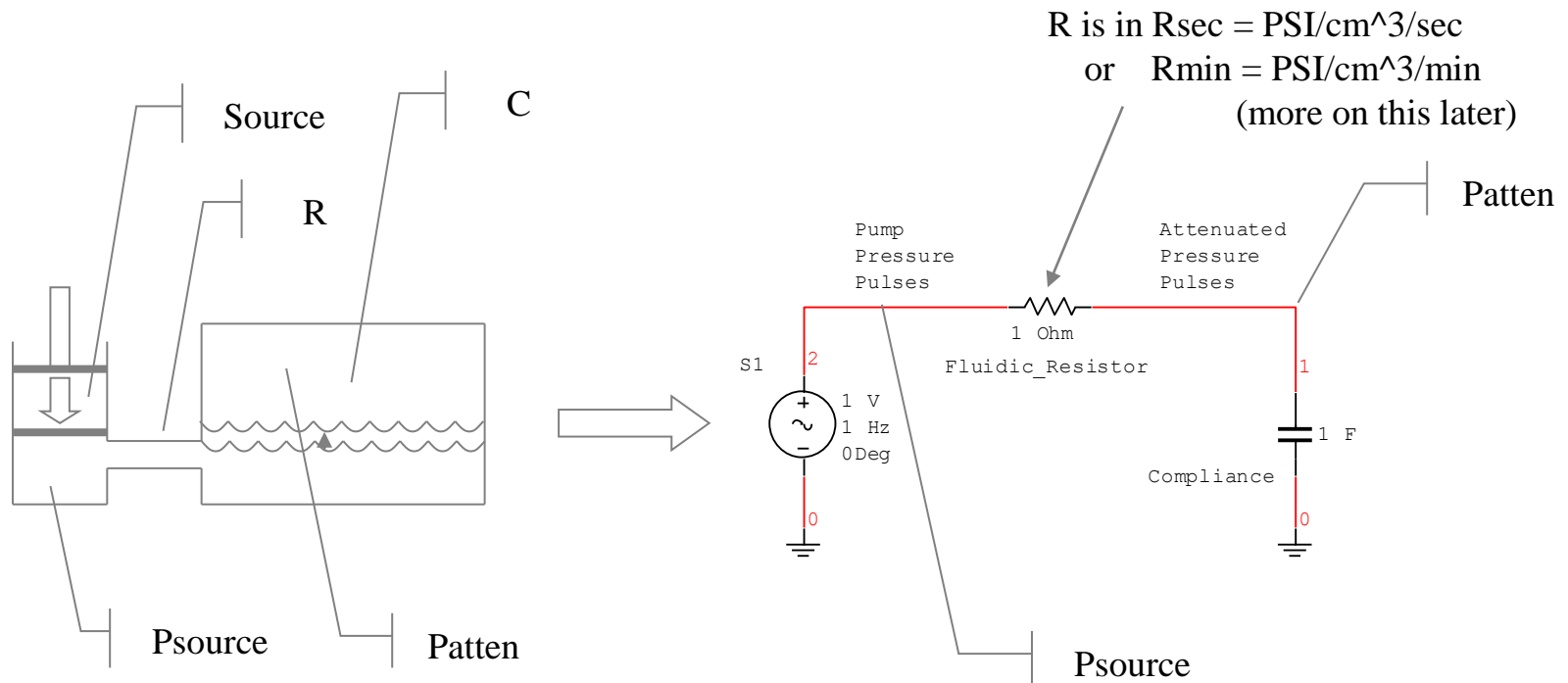
## Part II - Introduction

In the previous section, the compliant gas volume required to dampen pressure pulses to a desired amplitude was calculated. This can be thought of the “DC” or zero frequency of pressure excitation case. Now, using fluidic resistance and compliance as variable parameters, I will calculate the pressure response of the system as a function of frequency.



# Calculation Setup

Calculation of pressure pulse roll-off as a function of gas volume and series flow resistance is made easier by converting the system to its electrical analog ... a series-shunt "RC" network.



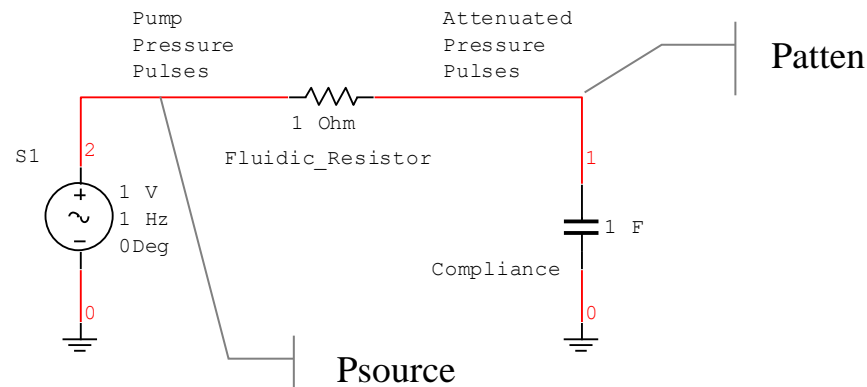
# Complex Attenuation Amplitude

From basic network theory, Patten (having some magnitude and phase relative to Psource) is given by:

$$P_{atten} = 1 / (R_{seconds} * C * \omega * j + 1) \quad \text{Complex Frequency Response}$$

Where:  $\omega$  is angular frequency in radians/sec  $\omega = 2 * \pi * \text{frequency}$   
 $j$  is the square root of -1

and  $R_{seconds}$  is fluidic resistance in (Pressure / FlowRate) in PSI / (cm<sup>3</sup>/sec)  
 $C$  is compliance in (delta Volume / delta Pressure) in delta cm<sup>3</sup> / delta PSI



If  $R_{sec} = 1$  then:  
 A flow of 1 cm<sup>3</sup>/sec through  $R_{sec}$  will cause a pressure drop of 1 PSI across  $R_{sec}$

# Magnitude of Attenuation – Rminutes Units

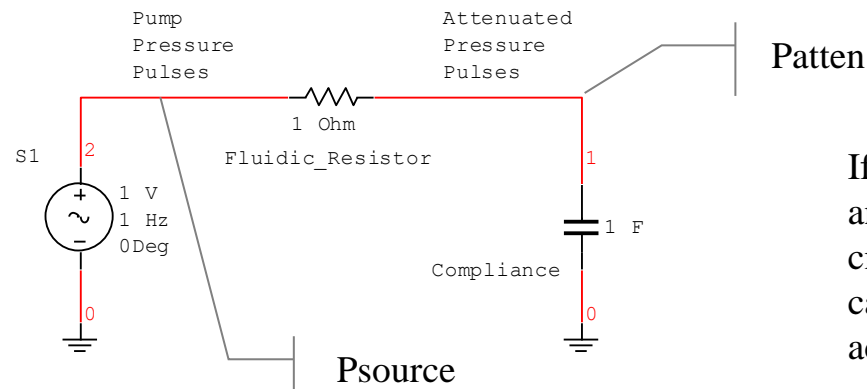
It is now useful to convert from Rseconds and angular frequency to Rminutes and frequency:

The magnitude of  $P_{atten}(freq) = 1 / (2 * \pi * freq * R_{min} * C * freq * j / 60 + 1)$

is (by algebra):  $|P_{atten}(freq)| = 1 / \sqrt{(2 * \pi * freq * R_{min} * C * freq / 60)^2 + 1}$

Where: frequency is in  $sec^{-1}$   $j$  is the square root of -1

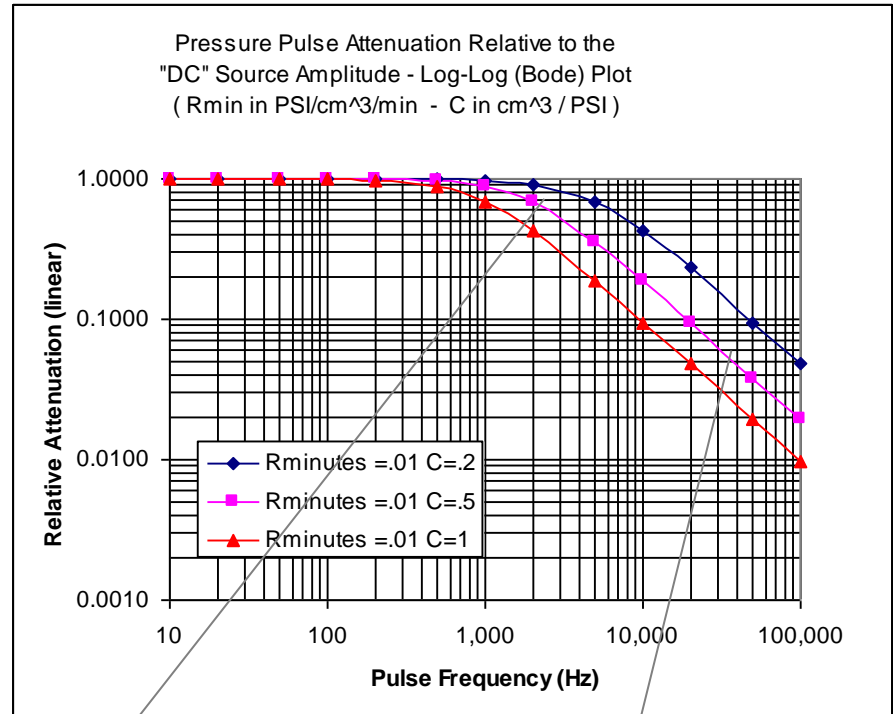
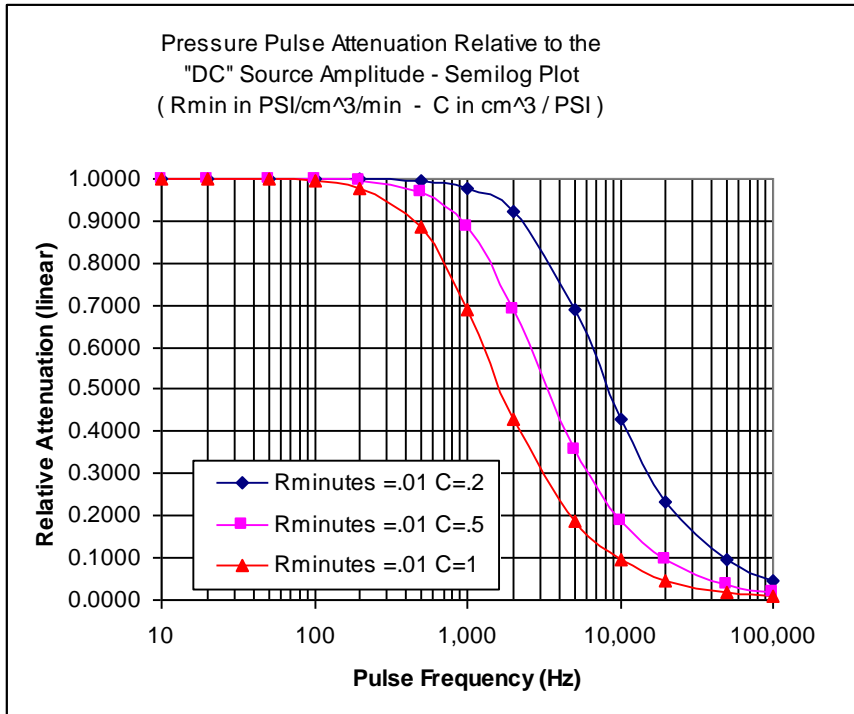
And  $R_{minutes}$  is fluidic resistance (Pressure/Flow rate) in  $PSI / (cm^3/min)$   
 $R_{seconds} = R_{min} / 60$   
 $C$  is compliance ( $\Delta$  Volume /  $\Delta$  Pressure) in  $\Delta cm^3 / \Delta PSI$



If  $R_{min} = 1$  then:  
 an average flow of 1  $cm^3/min$  through  $R_{min}$  will cause a pressure drop of 1 PSI across  $R_{min}$

# Magnitude of Attenuation ( $R_{min} = .01$ $C = .2, .5, 1$ )

The roll-off would be the same if  $C$  was held at  $.01$  and  $R_{minutes}$  varied from  $.2$  to  $.5$  to  $1$

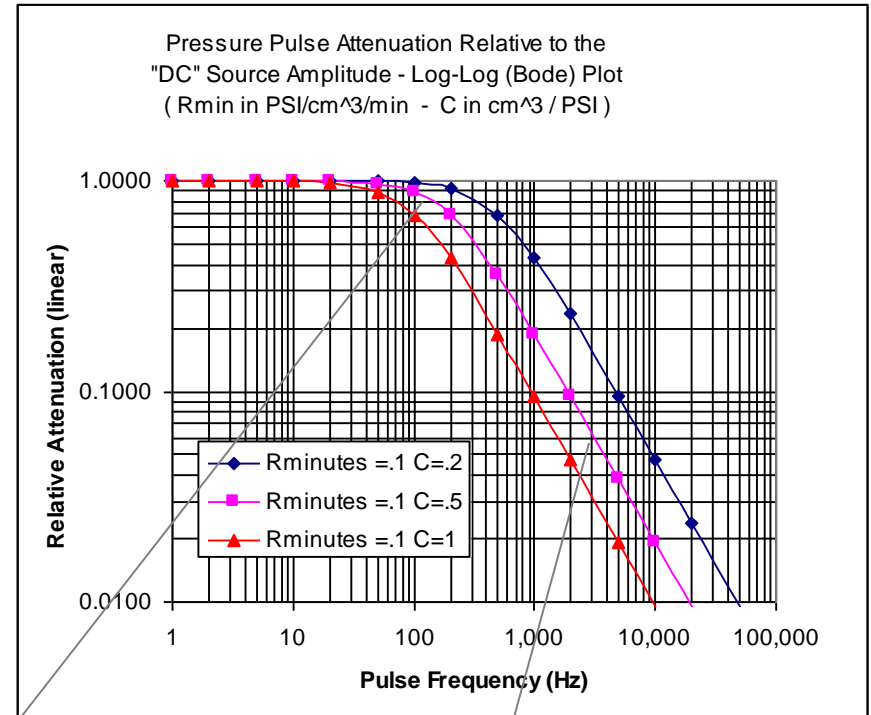
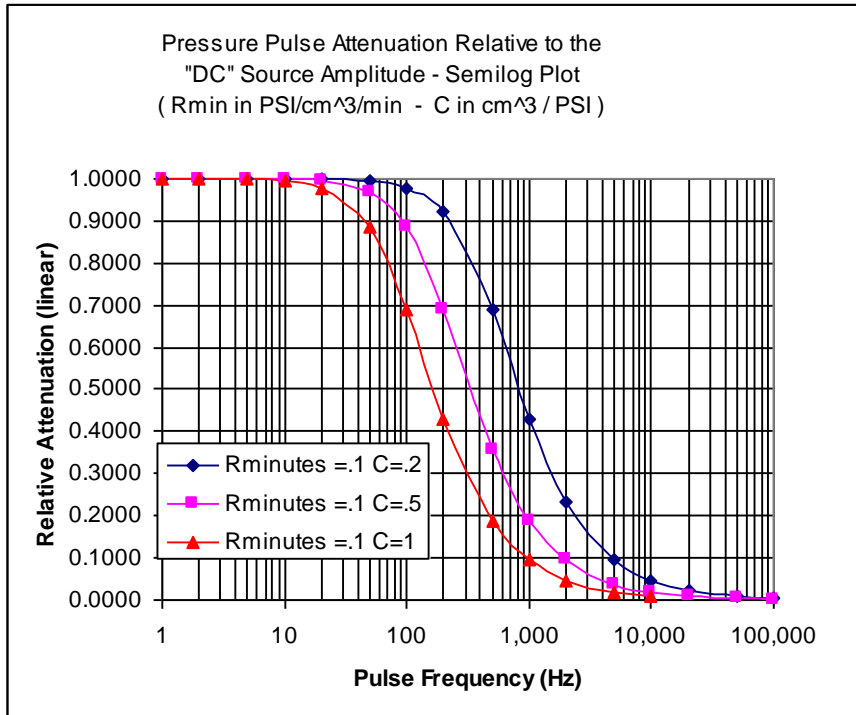


Corner frequency goes from about 1000 to 5000 Hz

x 10 Roll-off per decade of frequency increase

# Magnitude of Attenuation (Rmin =.1 C=.2,.5,1)

The roll-off would be the same if C was held at .1 and Rminutes varied from .2 to .5 to 1

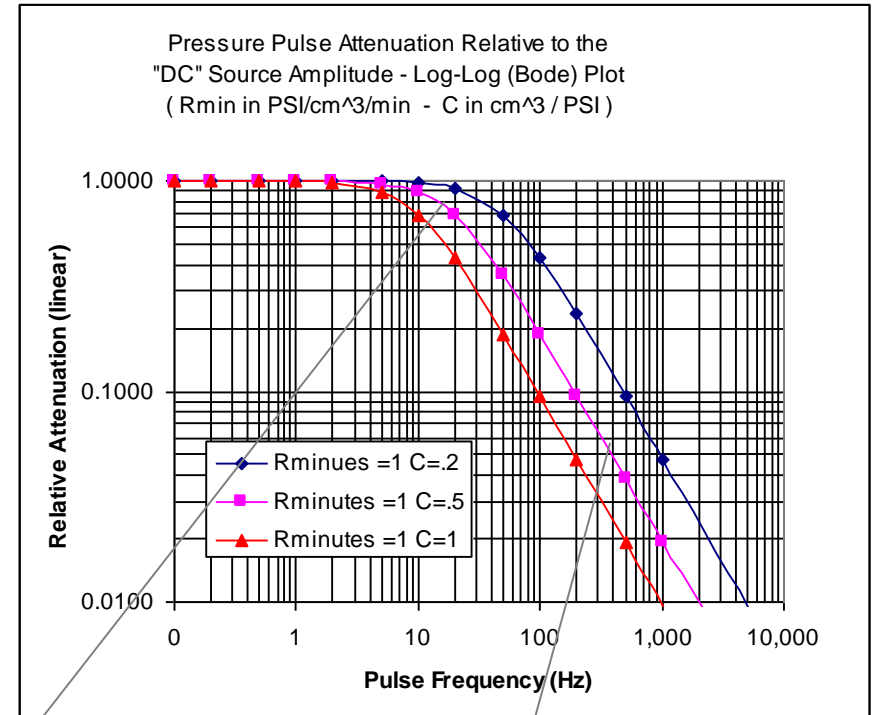
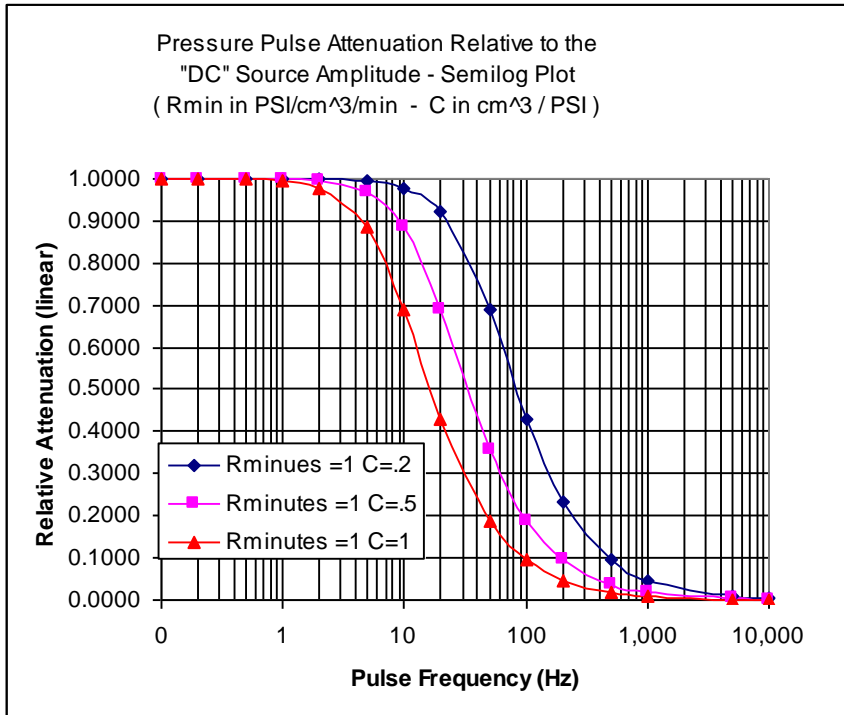


Corner frequency goes from about 50 to 500 Hz

x 10 Roll-off per decade of frequency increase

# Magnitude of Attenuation ( $R_{min} = 1$ $C=.2,.5,1$ )

The roll-off would be the same if  $C$  was held at 1 and  $R_{min}$  varied from .2 to .5 to 1



Corner frequency goes from about 5 to 50 Hz

x 10 Roll-off per decade of frequency increase

## Conclusions – Part II

1. With the high flow rates (50 ml/min), a series fluidic resistance large enough to be helpful filtering out pressure pulses will induce too much static pressure drop to be useful.
2. Dividing the total flow into many parallel flow channels with separate pulse dampeners for each channel would help the situation quite a bit.
3. The best answer is to seek out or develop small pumps that do not generate the relatively high pressure and low frequency pulses that the Model XYZ diaphragm pumps do.
4. In the mean time, two pressure pulse dampeners of approximately 9 cm<sup>3</sup> internal air volume, for each 50 ml/min flow loop, seem to be required for adequate pressure pulse dampening.